

Enhanced battery model including temperature effects

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Abstract

Within electric and hybrid vehicles, batteries are used to provide/buffer the energy required for driving. However, battery performance varies throughout the temperature range specific to automotive applications, and as such, models that describe this behaviour are required.

This paper presents a dynamic battery model describing the battery voltage based on current and temperature. A model identification method is presented and validation tests are performed. The results show that when temperature influences are included in the models, a significant increase in performance can be achieved. Modelling errors lower than 5% are achieved for validation tests conducted at -10°C, 0°C and 10°C, whereas the models that do not consider temperature show errors up to 10%.

Keywords: lithium battery, battery model, battery SoH

1 Introduction

With the scarceness of fossil fuels and the stringent emission regulations that are being put in place, hybrid (HEVs) and electric vehicles (EVs) are being developed at an increased pace. EVs rely on batteries for providing the energy required for driving, while HEVs use batteries for temporary energy storage during driving with the goal of optimizing fuel efficiency and/or increasing performance.

The high production cost of batteries, together with their inherent characteristics (the nonmeasurable nature of important parameters) motivated a great deal of research on battery modelling and state estimation ([1] [2] [3] [4] [5] [6] [7] [8]).

Temperature plays an important role in the behaviour of the battery, both on longer and shorter time scales. It is recognized that temperature affects the present battery performance [1]. Its effects on a longer scale, relevant to battery ageing phenomena, have also been reported in literature ([9] [10] [11] [12] [13]).

For range prediction, an important information is the amount of energy the battery can provide/receive. Energy management strategies re-

quire an accurate description of the power losses occurring within the battery, so that the most cost effective energy source (in the case of hybrid vehicles) is used at every moment. In the case of regenerative braking, the charge acceptance of the battery is extremely relevant, as it directly affects the required split between standard (mechanical) and regenerative braking. Different charging strategies (faster or slower home charging, on route charging, etc.) can be developed considering the trade-off between user requirements (having enough energy in the battery at a specified moment in time) and cost efficiency (balancing between the variable grid prices and considering battery ageing behaviour).

For all these applications, it is important to have a good mathematical description of how the battery operates. In this work, the electrical battery model presented in [8] is extended to include temperature effects. A model identification procedure is presented and validation tests are performed.

This paper is built up as follows. Section 2 describes the battery model developed in this work. The model identification procedure is presented in Section 3, while Section 4 describes the experimental results and the validation phase. In

$$\begin{pmatrix} SoC_k \\ V_{1,k} \\ V_{2,k} \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 - \frac{\Delta t}{R_1 C_1} & 0 \\ 0 & 0 & 1 - \frac{\Delta t}{R_2 C_2} \end{pmatrix} \begin{pmatrix} SoC_{k-1} \\ V_{1,k-1} \\ V_{2,k-1} \end{pmatrix} + \begin{pmatrix} \frac{\Delta t}{C_n} \\ \frac{\Delta t}{C_1} \\ \frac{\Delta t}{C_2} \end{pmatrix} I_{bat,k-1}$$

$$V_{bat,k} = V_{oc}(SoC_k, T_k) + V_{1,k} + V_{2,k} + R_0(SoC_k, T_k) I_{bat,k} \quad (1)$$

$$V_{oc}(SoC, T) = \kappa_0 + \alpha_0 T + \frac{\kappa_1}{SoC} + \alpha_1 T SoC + \kappa_2 SoC + \alpha_2 T \ln(SoC) + \underbrace{\kappa_3 \ln(SoC) + \alpha_3 T \ln(1 - SoC) + \kappa_4 \ln(1 - SoC)}_{f_1(SoC, T)} \quad [V], \quad (2)$$

$$R_0(SoC, T) = \underbrace{\begin{cases} (\gamma_0^+ + \dots + \gamma_{cO}^+ SoC^{cO})(\nu_0^+ + \dots + \nu_{c1}^+ T^{c1}), & \text{if } I_{bat,k} \geq 0 \\ (\gamma_0^- + \dots + \gamma_{dO}^- SoC^{dO})(\nu_0^- + \dots + \nu_{d1}^- T^{d1}), & \text{if } I_{bat,k} < 0 \end{cases}}_{f_2(SoC, T)} \quad [\Omega], \quad (3)$$

Section 5, concluding remarks are given.

2 Battery model considering temperature effects

The existing battery model was developed in [8] and is shown in Figure 1. It consists of an ideal voltage source, V_{oc} [V], which is State-of-Charge (SoC) dependent, an internal resistance R_0 [Ω], SoC dependent and different for charging and discharging, and two RC blocks, used to mimic the dynamic behavior of the battery. For more in depth information about battery dynamic behavior, the interested reader is referred to [1].

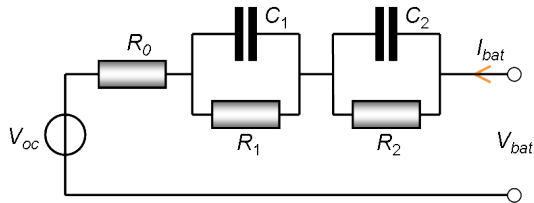


Figure 1: Dynamic battery model

A hybrid approach is followed to introduce temperature dependence in the existing battery model. The procedure consists of a mixture between physical and phenomenological battery modelling. The physical considerations originate from electrochemical battery modelling (see [14]) whereas electric circuit components were used to emulate the observed battery behavior. The resulting model has the same outline as the one shown in Figure 1. It is written in state space form in equation (1), with battery current I_{bat}

[A] as input and battery voltage V_{bat} [V] as output. The states of the model are the SoC and the voltages of the two RC blocks. The state-space model is written in discrete time. The sampling time is Δt [s] and the battery capacity is C_n [As]. The temperature effects are included in the open circuit voltage (V_{oc}) and internal resistance (R_0) respectively.

Equation (2) shows the dependence of the open circuit voltage on battery State-of-Charge and temperature, with $\kappa_{0:4}$ and $\alpha_{0:3}$ unknown parameters.

The dependence on temperature and SoC of the internal resistance is described by equation (3), where γ and ν are unknown parameters, different for charging and discharging. The order of the SoC polynomial is cO (charging) and dO (discharging) while the temperature polynomial is of order $c1$ (charging) and $d1$ (discharging).

3 Model identification procedure

For the identification procedure presented in this chapter it is assumed that the battery voltage, current and temperature are measured with a sample frequency of at least 1 Hz.

Figure 2 presents a discharge cycle used for the model characterisation. It originates from a LiFePO₄ battery module with a nominal voltage of 26.5 V and a nominal capacity of 160 Ah.

The design of the test cycle (consisting of current pulses of different amplitudes), allows identification of the internal resistance from the instantaneous change in battery voltage as a result of a stepwise change of the current, as it can be seen in Figure 3, at time value 100s.

The internal resistance can then be computed as:

$$R_0 = \frac{\Delta V}{I_{step}} \quad [\Omega], \quad (5)$$

$$H_R = \begin{bmatrix} 1 & \dots & SoC_1^{c0} & T_1 & \dots & T_1 SoC_1^{cO} & \dots & T_1^{c1} & \dots & SoC_1^{cO} T_1^{c1} \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ 1 & \dots & SoC_n^{c0} & T_n & \dots & T_n SoC_n^{cO} & \dots & T_n^{c1} & \dots & SoC_n^{cO} T_n^{c1} \end{bmatrix} \quad (4)$$

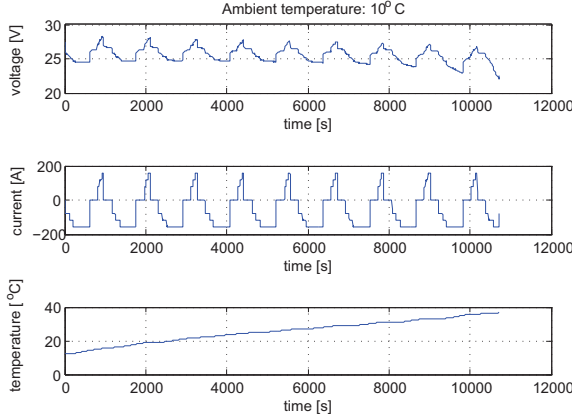


Figure 2: Discharge test with 10° C ambient temperature

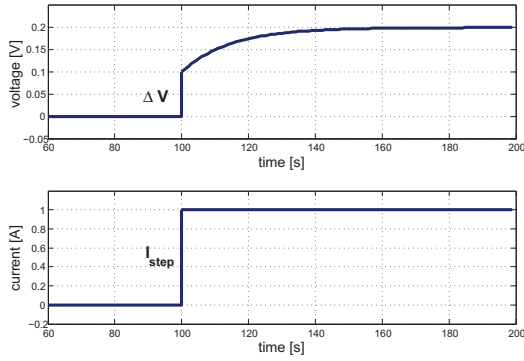


Figure 3: Step response

where ΔV [V] is the instantaneous step in voltage and I_{step} [A] is the amplitude of the current step.

After multiple values of the internal resistance have been computed, the unknown parameters of equation (3) can be identified using a least squares approach.

For each identified R_0 , the corresponding values of T and SoC were determined. The SoC is computed by integrating current, starting from a known initial value, according to the state update equation of the state space model presented in equation (1). Knowing these values, we can write equation (3) for each measurement point.

$$\underbrace{\begin{bmatrix} R_{0,1} \\ \vdots \\ R_{0,n} \end{bmatrix}}_{R_0} = \underbrace{\begin{bmatrix} f_2(SoC_1, T_1) \\ \vdots \\ f_2(SoC_n, T_n) \end{bmatrix}}_{H_R \Phi_R} \quad (6)$$

The equation above is valid for both the charging and the discharging internal resistance. For simplicity, only the charging case will be treated here. The discharging internal resistance can be determined analogously.

In equation (6), R_0 is the vector of the internal resistances whereas H_R depends only on temperature and SoC (see below) and Φ_R is the vector of the unknown parameters that are to be identified. The unknown parameters can be determined as the least squares solution of equation (6):

$$\Phi_R = (H_R^T H_R)^{-1} H_R^T R_0 \quad (7)$$

Please note that the elements of Φ_R are not exactly γ and ν from (3), but the results of the multiplications of the coefficients of the T and SoC polynomials of the same equation.

After the parameters describing the internal resistance have been identified, the voltage drop over R_0 is computed.

$$V_{R0} = \underbrace{H_R \times \Phi_R}_{R_0(SoC, T)} \times I_{bat} \quad (8)$$

In equation (8), $R_0(SoC, T)$ represents the identified internal resistance (the functional dependence shown in (3) with the identified parameters).

If equation (2) is written for each measurement point, the following is obtained:

$$\underbrace{\begin{bmatrix} V_{oc,1} \\ \vdots \\ V_{oc,n} \end{bmatrix}}_{V_{oc}} = \underbrace{\begin{bmatrix} f_1(SoC_1, T_1) \\ \vdots \\ f_1(SoC_n, T_n) \end{bmatrix}}_{H_V \Phi_V} \quad (9)$$

H_V can be computed based on T and SoC : The unknown parameters are then given by the least squares solution:

$$\Phi_V = (H_V^T H_V)^{-1} H_V^T V_{oc} \quad (11)$$

At this point, the internal voltage cannot be independently determined. However, the sum between V_{oc} and the voltage drops over the two RC blocks can be computed.

$$H_V = \begin{bmatrix} 1 & T_1 & \frac{1}{SoC_1} & T_1 SoC_1 & SoC_1 & T_1 \ln(SoC_1) & \ln(SoC_1) & T_1 \ln(1 - SoC_1) & \ln(1 - SoC_1) \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ 1 & T_n & \frac{1}{SoC_n} & T_n SoC_n & SoC_n & T_n \ln(SoC_n) & \ln(SoC_n) & T_n \ln(1 - SoC_n) & \ln(1 - SoC_n) \end{bmatrix} \quad (10)$$

$$V_{bat} - V_{R0} = \underbrace{V_{oc} + V_{rc1} + V_{rc2}}_{V_{dyn}} \quad (12)$$

Looking back at equation (1), it can be seen that the internal voltage is linearly independent of the voltage drops over the two RC blocks. This allows the use of V_{dyn} instead of V_{oc} for determining Φ_V :

$$\Phi_V = (H_V^T H_V)^{-1} H_V^T V_{dyn} \quad (13)$$

The internal voltage is then:

$$V_{oc} = H_V \times \Phi_V \quad (14)$$

The voltage of the two RC blocks can be computed as:

$$V_{rc1} + V_{rc2} = V_{dyn} - V_{oc} \quad (15)$$

At this point, the parameters describing the RC blocks can be identified using the method presented in [4].

4 Experiments and validation



Figure 4: Digatron BS-400 battery test system



(a) Climate chamber



(b) Battery pack

Figure 5: Test setup

To validate the proposed method, experimental tests were conducted on a battery pack produced

by Mastervolt (type MLi 24/160). The tests consisted on applying a sequence of current pulses of different amplitudes, both for charging and discharging. This was done under different ambient temperatures, ranging from -18°C to 40°C .

The charging and discharging of the battery

were performed with the Digatron BS-400 (programmable high voltage source and sink).

The different ambient temperatures were obtained by placing the Mastervolt battery (Figure 5b) inside a climate cabinet (Votsch VCS4033, see Figure 5a) which can accurately regulate ambient temperature and humidity.

Each test was started with a full battery, charged according to the CCCV (constant current constant voltage) procedure. To achieve repeatability, each charging event took place at an ambient temperature of 10°C and a battery temperature (at the start of the charge profile) of 35°C.

The tests were conducted at ambient temperatures of -18°C, -10°C, 0°C, 10°C, 25°C and 40°C. The battery temperature equaled the ambient temperature at the start of the tests. Starting from these measurements, the battery internal resistance R_0 as a function of temperature and SoC has been identified, as presented in Figure 7.

The red stars in the figure represent the values of R_0 identified directly from the step responses, on which the least-squares identification procedure is based. Significant temperature influences on the internal resistance can be seen.

Figure 6 presents the dependence of the internal voltage on temperature and SoC, which is obtained as a result of the model parameters identification procedure. The data points used for the identification routine can be seen in black.

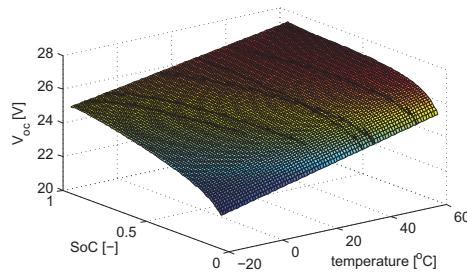


Figure 6: Identified internal voltage, as a function of temperature and SoC

Figure 8 shows a comparison between a model not including temperature influences (model presented in [8], identified using data measured at 25°C ambient temperature) and the model developed in this work. For simplicity, the model developed in [8] will be referred to as model 1, while the one proposed in this work, including temperature effects, as model 2. Three of the tests are analyzed, with data collected at -10°C, 0°C and 10°C ambient temperature. In each test case, for model 2, the data collected in the other 5 tests is used for model identification. The RC parameters were identified using the 25°C test, at SoC value of 0.5. For simplicity, these parameters were used for both models.

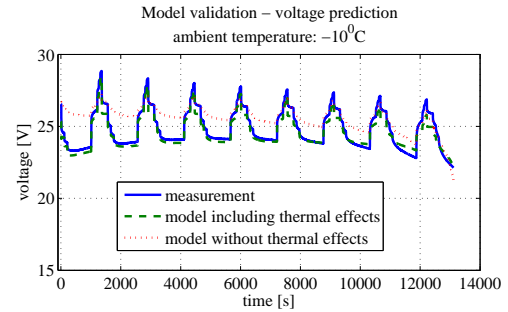
It can be seen that, as the temperature decreases, the accuracy gain of the model developed in this work increases. This is mostly the result of ac-

counting for the increase in the internal resistance due to lower temperature. In Figure 8a - ambient temperature of -10°C, the difference between the voltage prediction of the two models during current pulses (described in Figure 2) is significantly bigger than in Figure 8c - ambient temperature of 10°C.

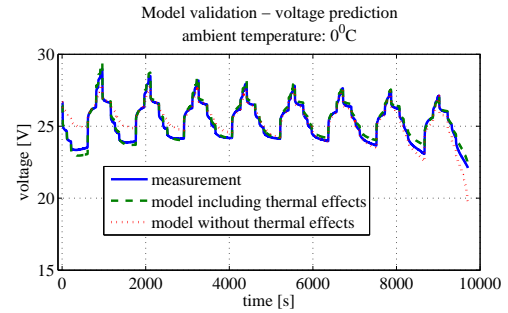
Figure 9 looks at the voltage prediction errors, expressed as percentile values - see equation (16). In all cases, it can be seen that including temperature effects in the model brings an important increase in performance.

$$error = \frac{V_{model} - V_{measured}}{V_{nominal}} \times 100 \quad [\%], \quad (16)$$

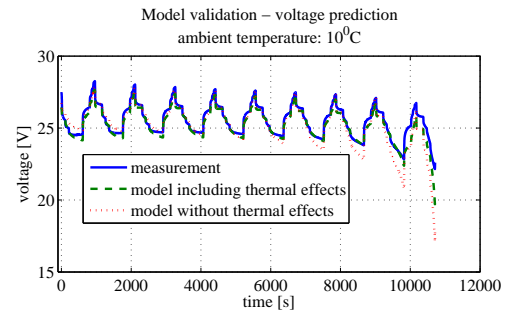
where $V_{nominal}$ is the nominal battery voltage, specified by the manufacturer.



(a) test 1



(b) test 2



(c) test 3

Figure 8: Voltage prediction at different temperatures

A closer look at the error characteristics shown in Figure 9 reveals some interesting aspects. At the beginning of the three cycles, the model which does not take into account temperature effects is conservative in estimating the voltage drops.

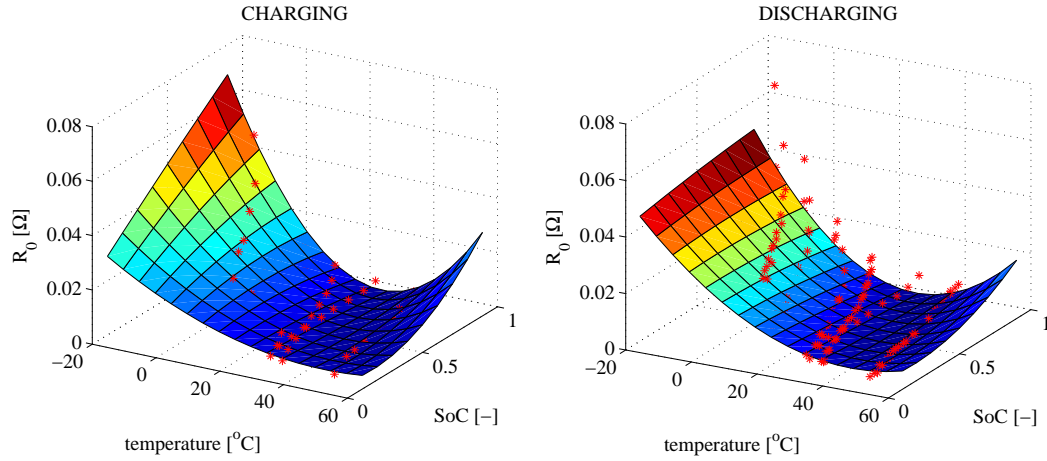


Figure 7: Identified internal resistance, as a function of temperature and SoC, for charging and discharging

This is due to the impedance increase with decreasing temperature. As the battery is discharged, a decrease is visible in the relative errors obtained by model 1. They start with high positive values at high SoC and decrease to low negative values for low SoC, not unlike the behaviour of the temperature during the tests (Figure 10 shows the battery temperature as a function of SoC for the 10° C test). This suggests that the errors of model 1 partly originate from not accounting for temperature.

For all three tests, Figure 9 shows that the errors of model 2 are more constant over the entire SoC range. The error shapes seem to suggest a temperature influence on the RC model parameters, which can be addressed as future work.

Overall, the figures show that a significant increase in voltage prediction accuracy can be achieved when temperature effects are taken into account by the model. Further accuracy increases are possible when temperature influences are considered for more model parameters.

5 Conclusions

In this work, a battery model including thermal effects has been developed, together with a model identification procedure. Coupled, the two show encouraging results, with voltage modelling errors smaller than 5%, compared to 10%, if temperature effects are not included.

Experimental tests suggest a strong temperature influence on the impedance characteristic of the battery. Information found in [14], where an electrochemical modelling approach is followed, backs up this assumption. The present work captures a part of this behaviour in the R_0 dependence on temperature. A direction to further improve the model accuracy is an investigation on the temperature and SoC effects on the RC parameters.

Nonetheless, in its present form, the temperature inclusion in the model offers a significant increase in voltage prediction performance. Sev-

eral applications will take full advantage of this increase of performance. On one side, range prediction algorithms for electric vehicles become more accurate over a wider range of environmental temperatures, while beneficial influences are also expected in model based energy management strategies for hybrid vehicles. Furthermore, smart regenerative braking algorithms gain a better insight into the charge acceptance of the battery over a wide temperature range.

For a number of applications (vehicle sizing and configuration analysis tools, controls development tools, battery second life applications, total cost of ownership (TCO) models), the ability to capture the ageing characteristics of automotive traction batteries is essential. The detrimental effect of higher temperatures on battery ageing is widely documented ([9] [10] [11] [12] [13]).

Impedance losses are an important source of the heat generated in the battery [15]. As the battery impedance changes with battery temperature, so does then its heat generation capability.

A coupled electro-thermal cell model has been developed to describe this behaviour. This model is then used as a building block in an electro-thermal battery pack model. The aim is to correctly describe the relevant stress factors (temperature, but also Depth-of-Discharge or current rates) for battery aging during the vehicle usage of the battery. The derived stress factors are then fed into battery aging models to assess the degradation of the battery pack.

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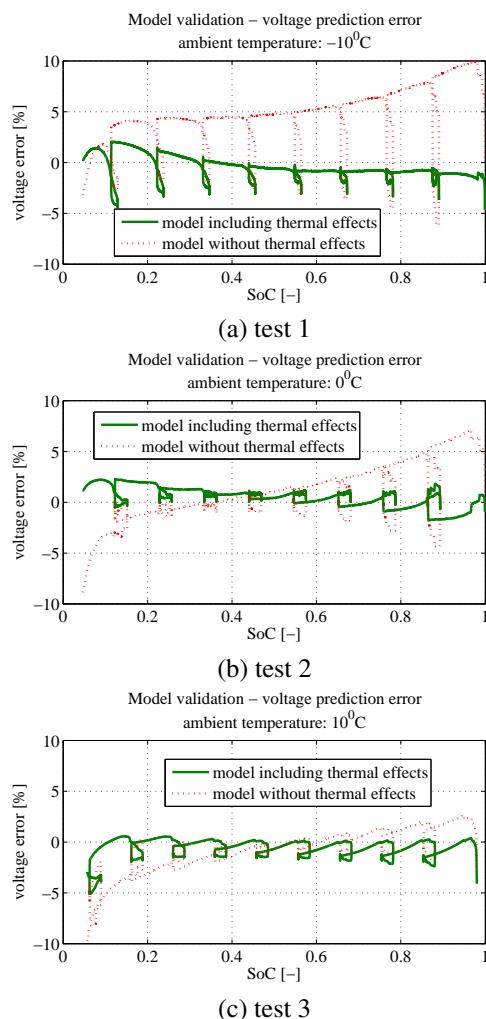


Figure 9: Voltage prediction errors at different temperatures

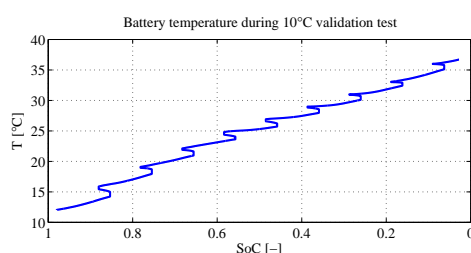


Figure 10: Battery temperature as a function of SoC during the 10° C test

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