

# A Model to Evaluate Coupled Driving-and-Charging Incentives for Electric Vehicles

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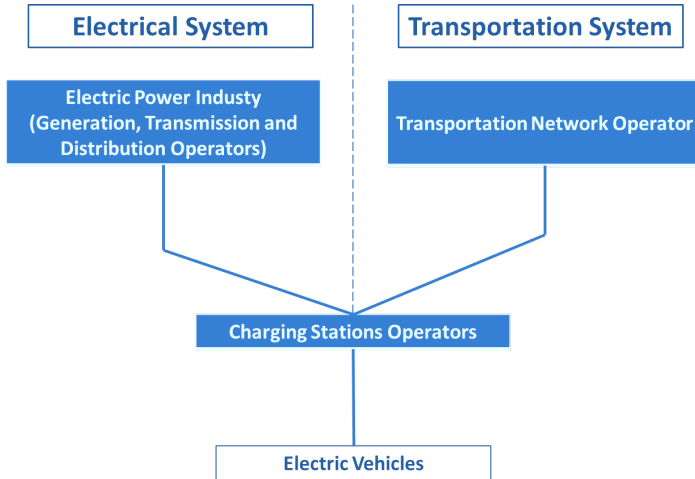
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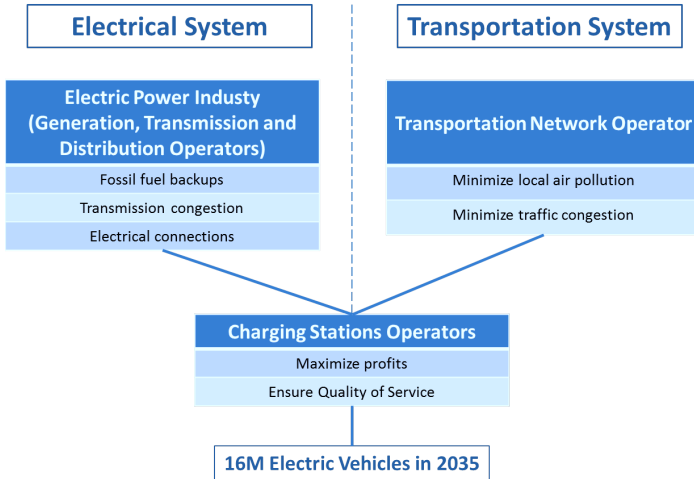
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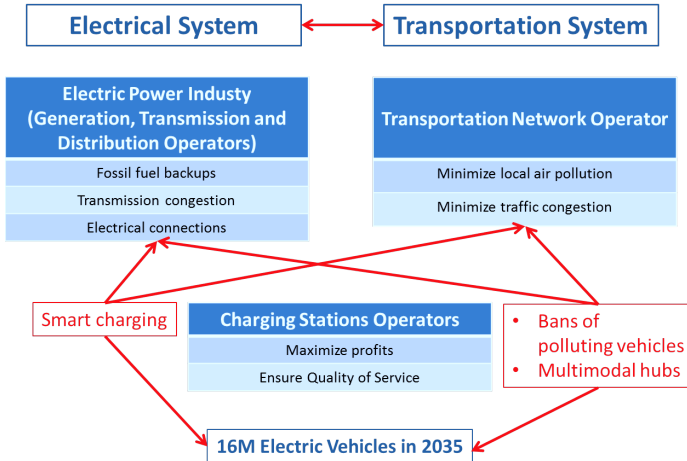
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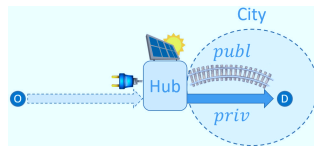
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# Scenario: e-Park & Ride hub

A group of **E**lectric and **G**asoline **V**ehicles (EV and GV) arrives at an e-Park & Ride hub. They can either:

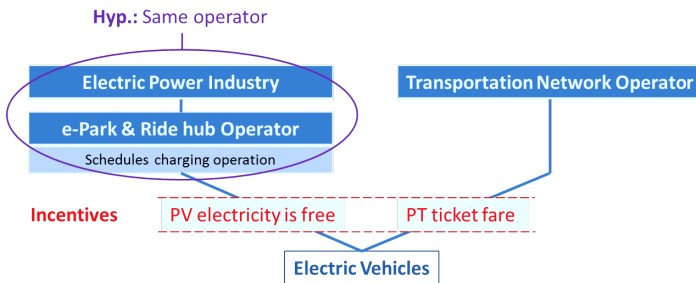
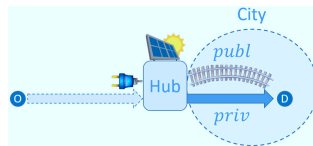
- 1 Park and charge at the hub with its **P**hoto**V**oltaic (PV) solar panels, and take **P**ublic **T**ransport (PT);
- 2 Drive all the way to the city center.



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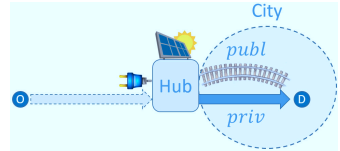
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# Model: Minimize duration and price

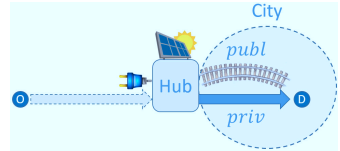
- publ* Pay for energy consumed to get to the hub and take Public Transport
- priv* Drive into congested city center and pay for total energy consumed



# Model: Minimize duration and price

*publ* Pay for energy consumed to get to the hub and take Public Transport

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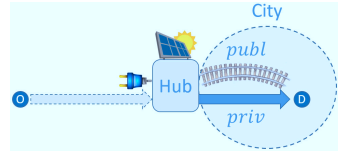
Transport mode	Travel duration	Consumption cost
Public	<ul style="list-style-type: none"><li>Constant</li></ul>	<ul style="list-style-type: none"><li>Charging price depends on EV nb</li><li>+ Constant PT fare</li></ul>
Private	<ul style="list-style-type: none"><li>Depends on vehicles nb (congestion)</li><li>→ BPR function</li></ul>	<ul style="list-style-type: none"><li>Constant (distance-dependent)</li></ul>



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## Equilibrium

Stable situation between strategic decision-makers

# Hub charging service

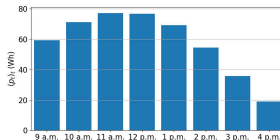
At the hub, the operator schedules the charging operation to minimize the costs related to peak demand.

- **Constraint:** Total charging need  $L_e$  ( $\propto$  EV nb at the hub)
- **Control:** Aggregated charging profile  $(\ell_{e,t})_t$   
s.t.  $\sum_{t=1}^T \ell_{e,t} = L_e$

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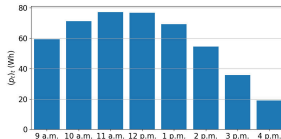
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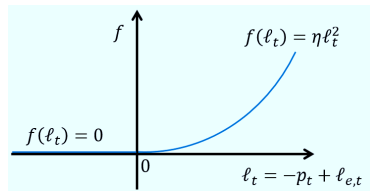
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- **Objective:** Minimize electricity distribution costs  $f$

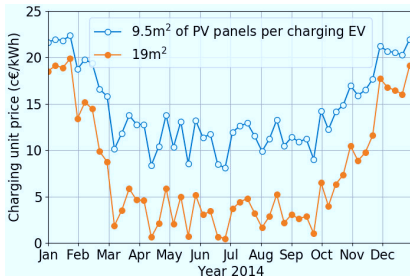


- Optimal aggregated charging profile  $\rightarrow$  Minimal distribution costs *val*
- Charging unit price =  $\frac{\text{Minimal distribution costs}}{\text{Aggregated charging need}} = \frac{\text{val}}{L_e}$

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- Charging unit price = 
$$\frac{\text{Minimal distribution costs}}{\text{Aggregated charging need}} = \frac{val}{L_e}$$



- PV panels located in Paris<sup>a</sup>
- Hub charging service cheaper from March to October
- Depending on nb of EV at the hub, charging may be free or not (see end of June)

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<sup>a</sup><https://www.renewables.ninja/>

# Sensitivity analysis: Public Transport fare

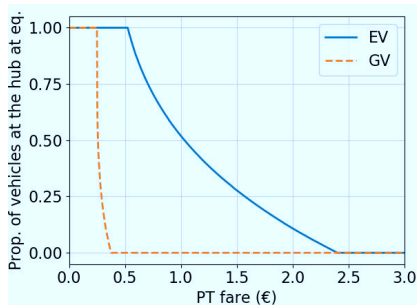


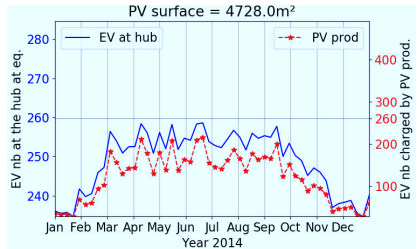
Figure: Equilibrium computed for any PT fare

- More EV than GV at the hub thanks to charging incentives (PhotoVoltaic production provided for free)
- ↘ 0.50€ Public Transport fare → +25% of EV at the hub

# Sensitivity analysis: PhotoVoltaic surface

## Parameters

- Total number of EV = 500
- PT fare = 1€  
→ no GV at the hub at eq.



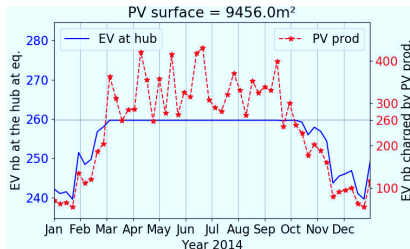
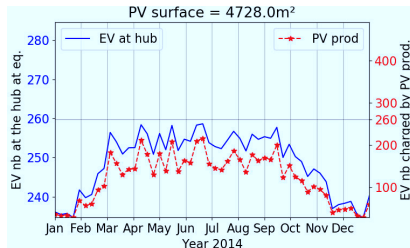


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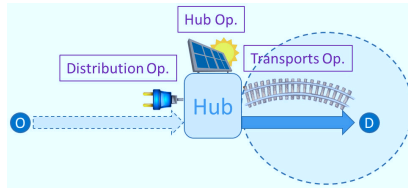
## Parameters

- Total number of EV = 500
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- EV may charge at the hub even if it is not free
- EV may charge downtown even if it is free at the hub



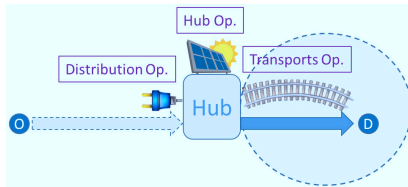
# Conclusion



## Summary

- **Model:** EV **coupled** behavior while driving and charging
- **Scenario:** Multimodal hub with PhotoVoltaic production
- **Use:** Design of Public Transport fare and PV surface

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## Perspectives

- EV choose charging need and departure time
- Accurate model of electricity distribution costs
- Definition of operators' utilities and game between them

# Appendix 1

Transport mode	Duration	Price	Vehicle class
Public	$\tau_{publ} \times d_{publ}$	$l_{publ} m_e \lambda_e(x_{e,publ}) + t_{publ}$	EV
		$l_{publ} m_g \lambda_g + t_{publ}$	GV
Private	$\tau_{priv} \times \frac{l}{v} (1 + 2x_{priv}^4)$	$l_{priv} m_e \lambda_e^0$	EV
		$l_{priv} m_g \lambda_g$	GV