

**NISSAN**  
**MOTOR CORPORATION**

# Vertical vibration reduction by new electric motor control in dry sand condition

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# Outline

- 1. Introduction
- 2. Vertical vibration under dry sand condition
  - Electric vehicle behavior
  - Vertical vibration simulation model
- 3. Vertical vibration motor control and effect
- 4. Summary

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# 1. Introduction

- Torsional vibration reduces comfort during riding.
- We proposed a vibration motor control method for EVs.

## <EV characteristics>

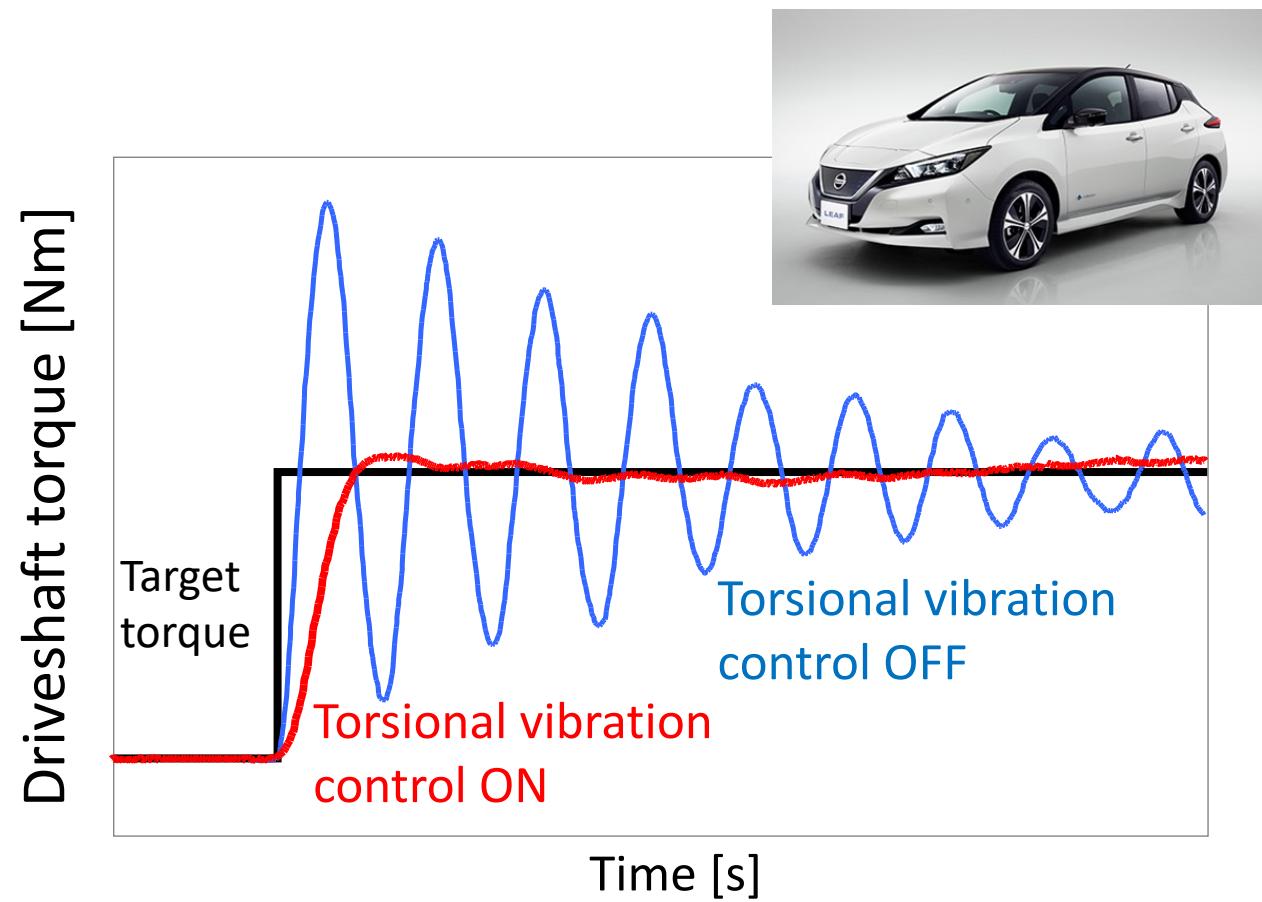
- High torque response
- High torque accuracy

## <Stiffness of driveshaft>

- Steep torque input to produce torsional vibration

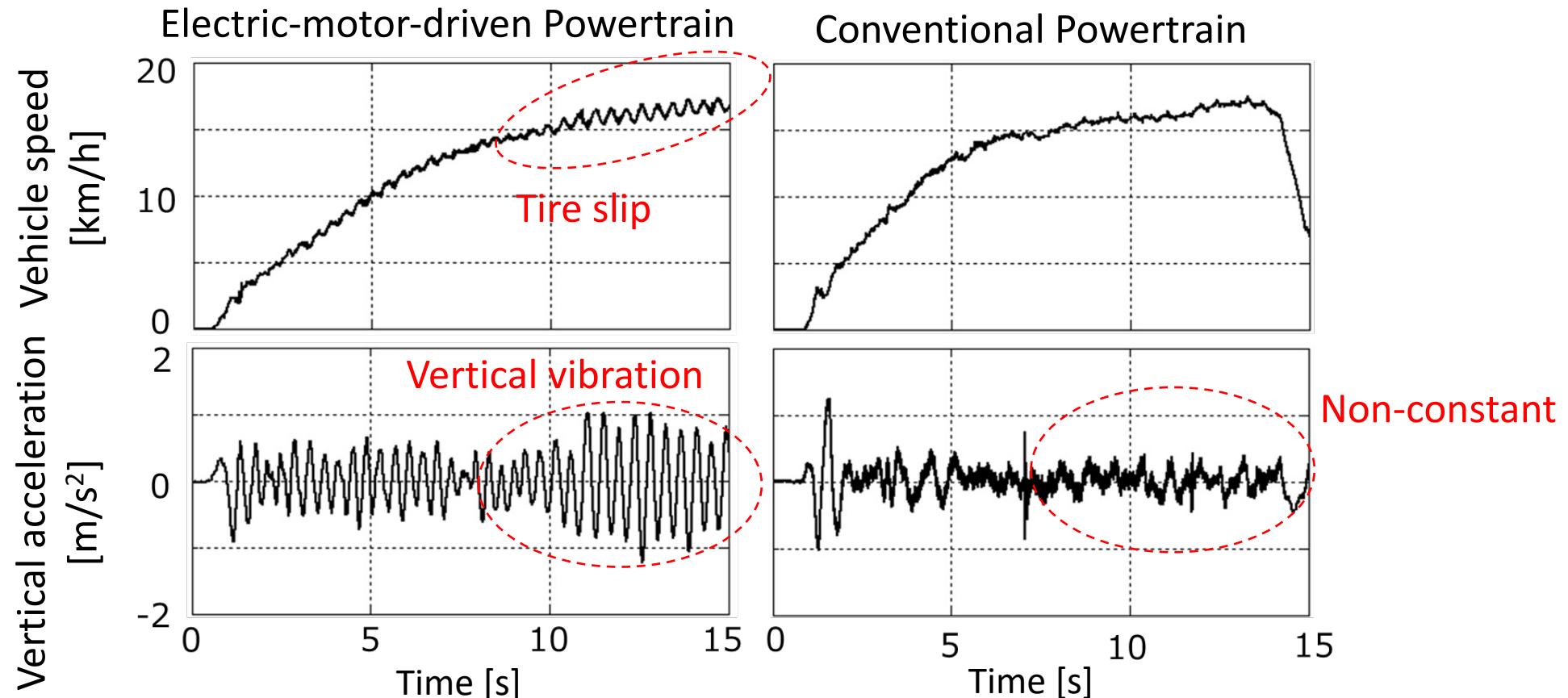


Torsional vibration control



# 1. Introduction

- Electric-motor-driven vehicle not avoid vertical vibration under dry sand condition.

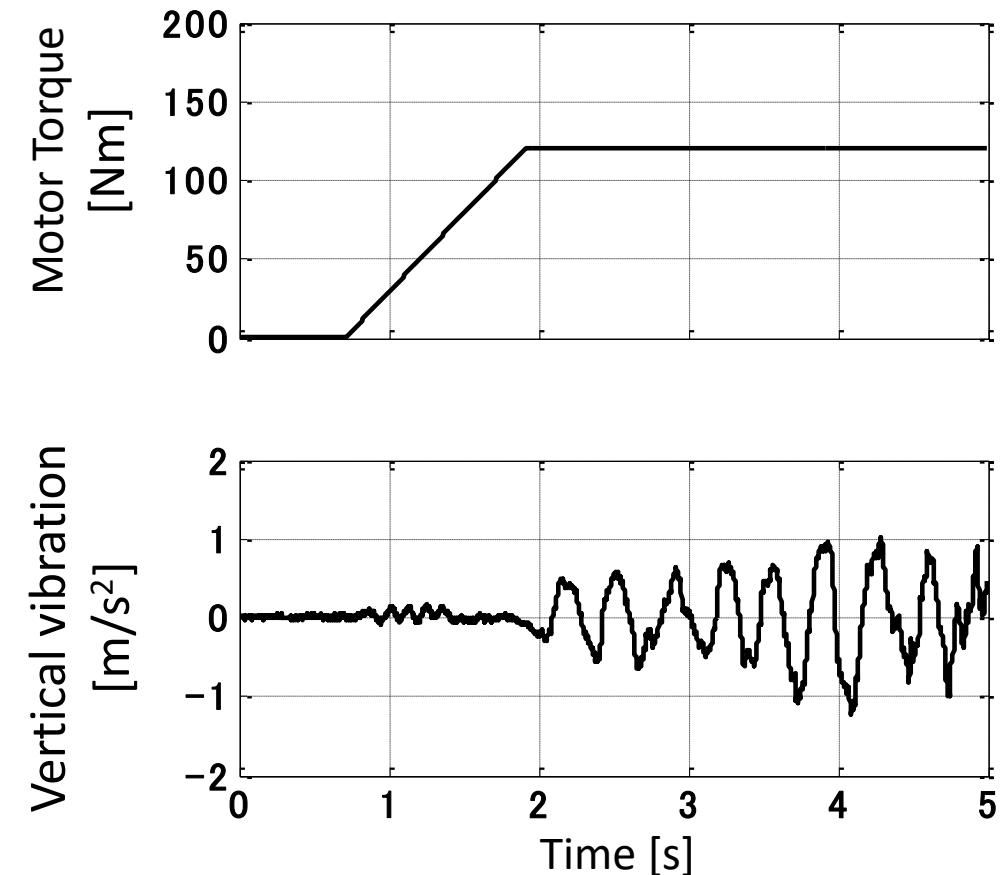


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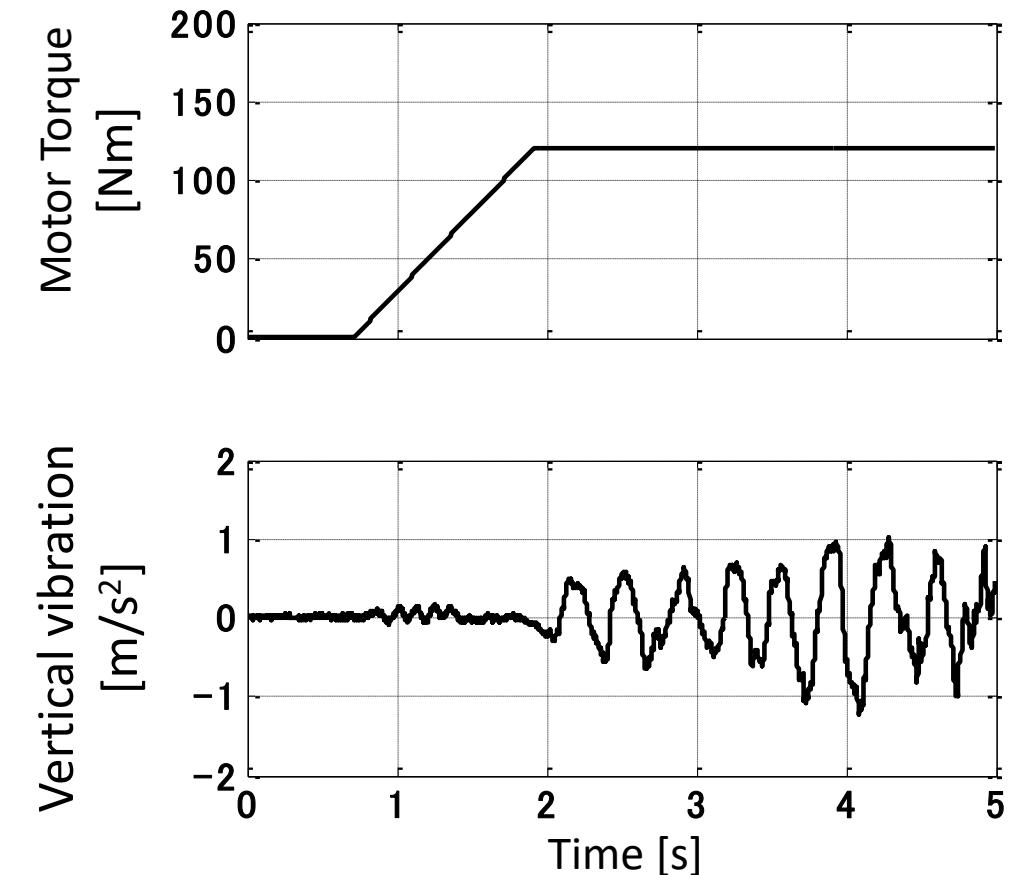
## 2. Vertical vibration-EV behavior under dry sand condition

- Tires sink in dry sand depending on wheel load.
- Motor torque is constant, but Car body only vertical vibrates.



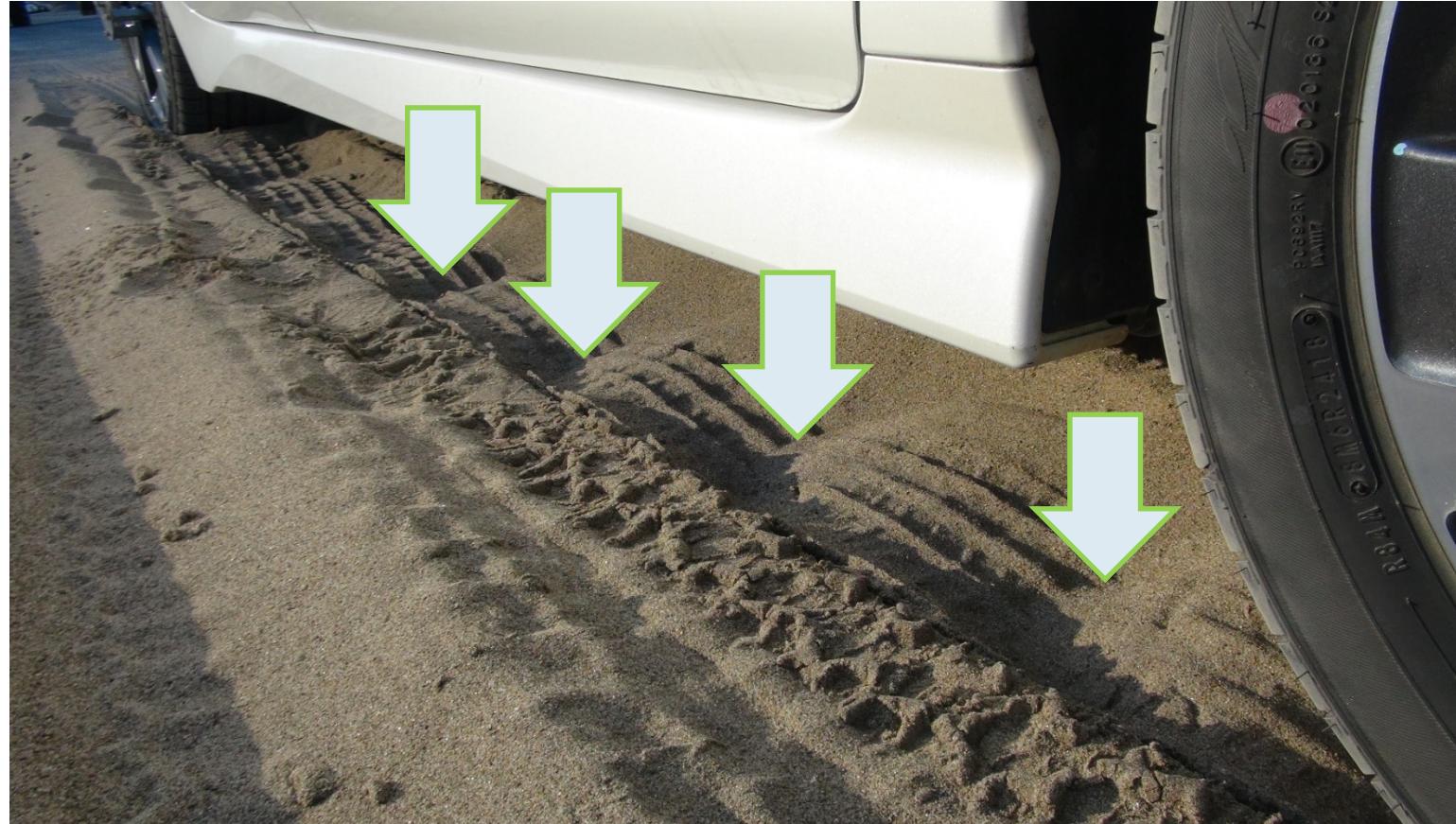
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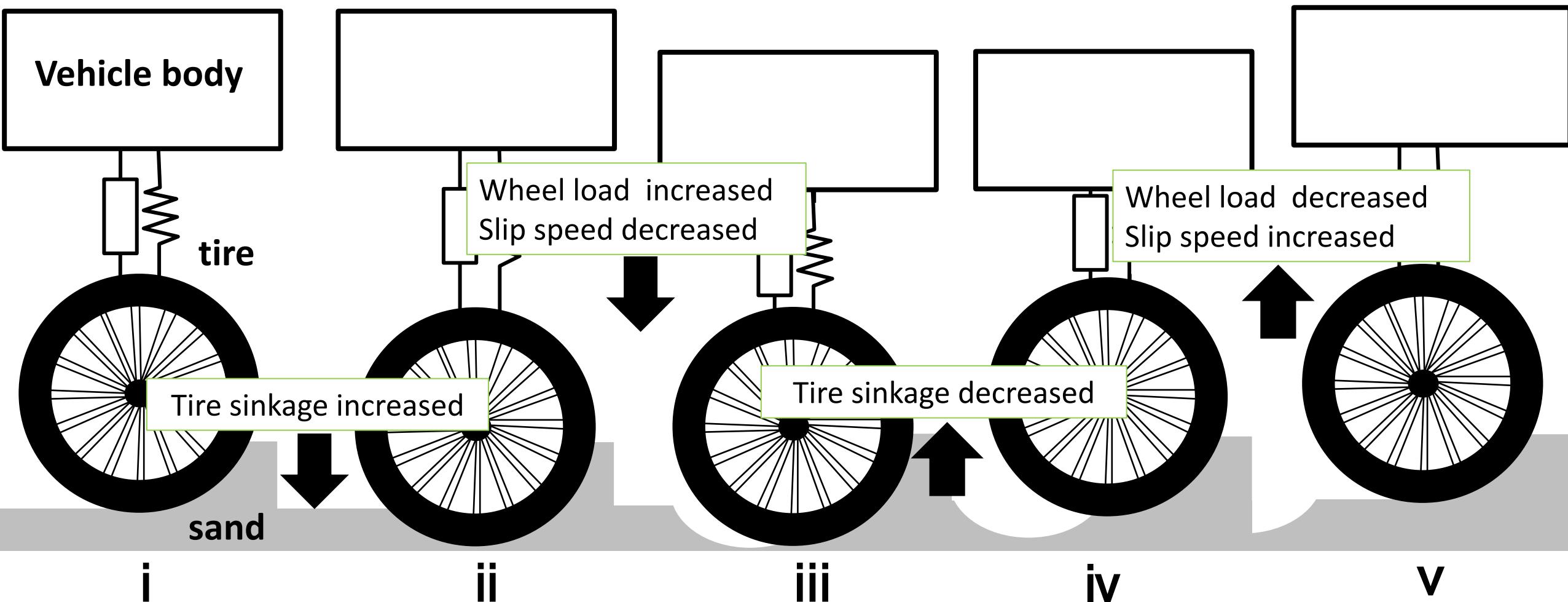
## 2. Vertical vibration-EV behavior under dry sand condition

- Trajectory of the dents can be observed, and the tires are sinking.



## 2. Vertical vibration-EV behavior under dry sand condition

- The vertical movement of the drive wheel is related to the vertical vibration of the vehicle body.

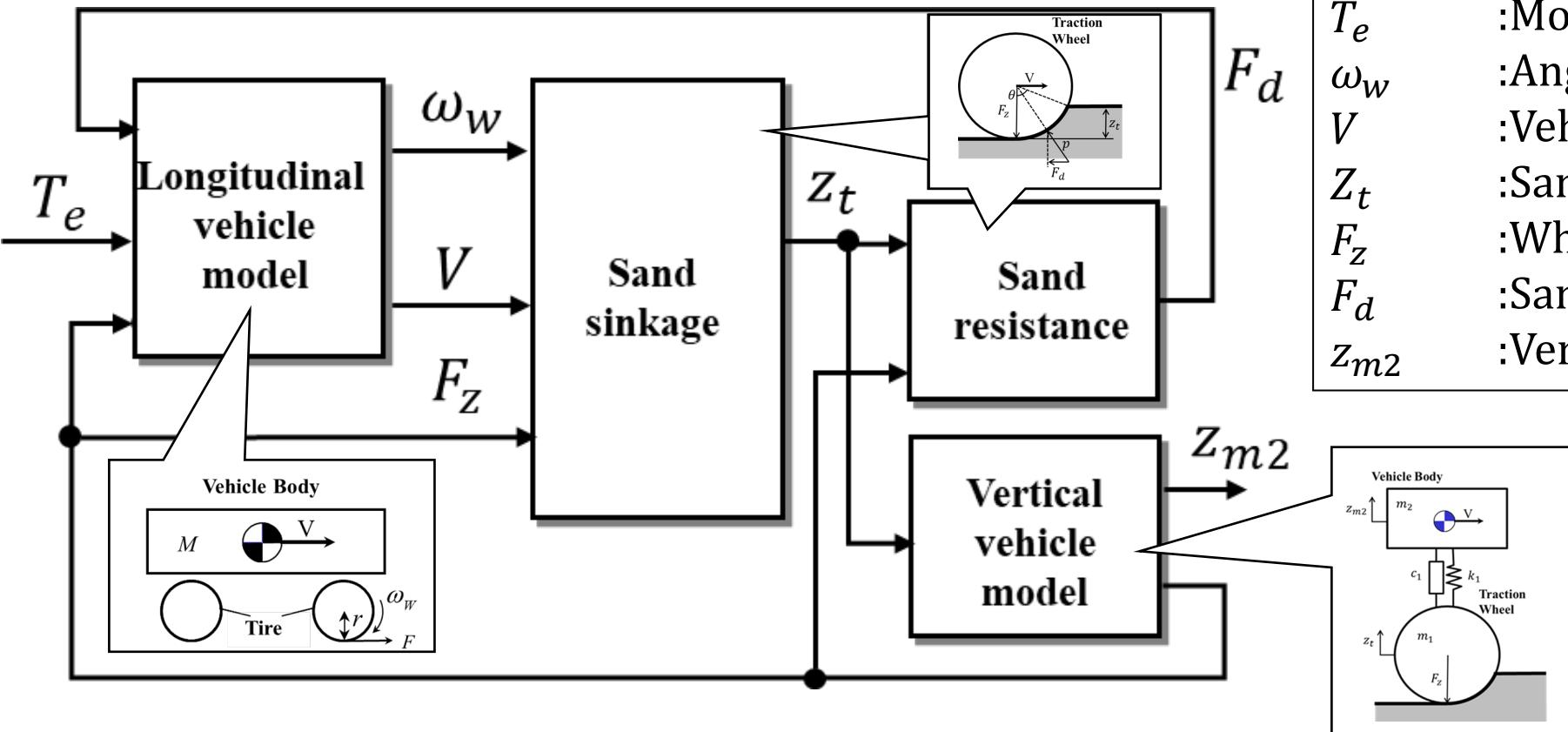


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## 2. Vertical vibration-Vertical vibration simulation model

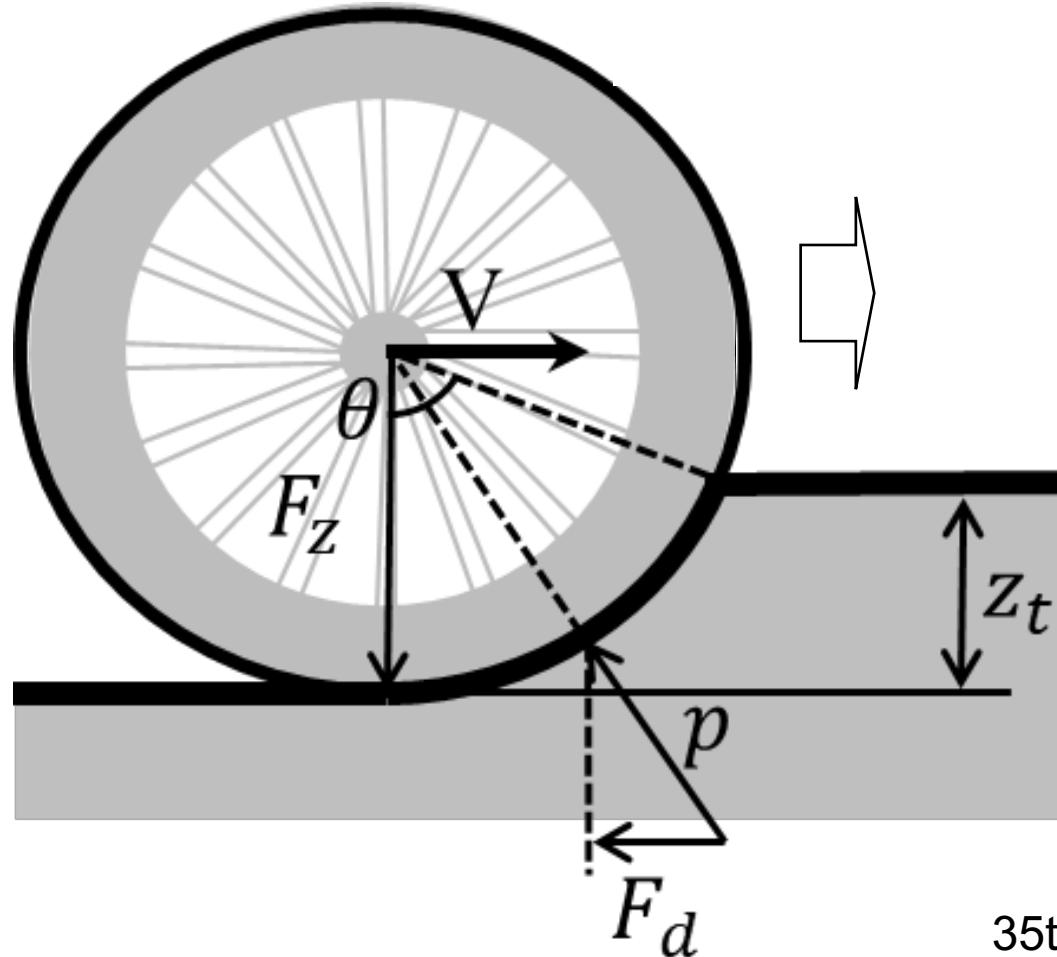
- To make a driving force transmission system model focusing Sand sinkage and Sand resistance and vertical motion.



$T_e$	:Motor torque
$\omega_w$	:Angular velocity of drive wheel
$V$	:Vehicle velocity
$Z_t$	:Sand sinkage
$F_z$	:Wheel load
$F_d$	:Sand resistance
$z_{m2}$	:Vertical displacement of body

## 2. Vertical vibration-Vertical vibration simulation model

- The sand sinkage ( $z_t$ ) exhibits transient response on dry sand.
- The sand resistance ( $F_d$ ) is calculated using  $z_t$ .



$z_t$ : Sand sinkage

$s$ : Laplace operator

$$z_t = \frac{1}{\tau_z s + 1} z_{max}$$

$z_{max}$ : transient and steady sinkage  
 $\tau_z$  : transient response parameter

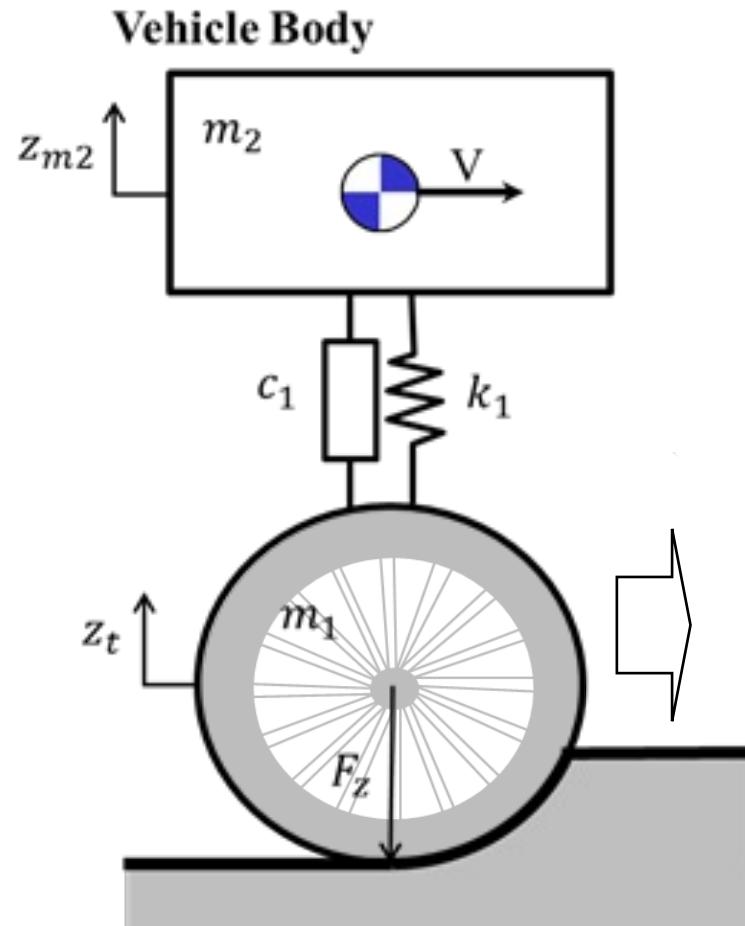
$F_d$ : Sand resistance

$$F_d = f(z_t) + g(F_z)$$

$f(z_t)$ : Sand resistance factor  
 $g(F_z)$ : Road friction coefficient

## 2. Vertical vibration-Vertical vibration simulation model

- Vertical displacement of body ( $z_{m2}$ ) is calculated based on the suspension characteristics and wheel load.



$z_{m2}$ : Vertical displacement

$$z_{m2} = \frac{c_1 s + k_1}{m_2 s^2 + c_1 s + k_1} z_t$$

$s$ : Laplace operator

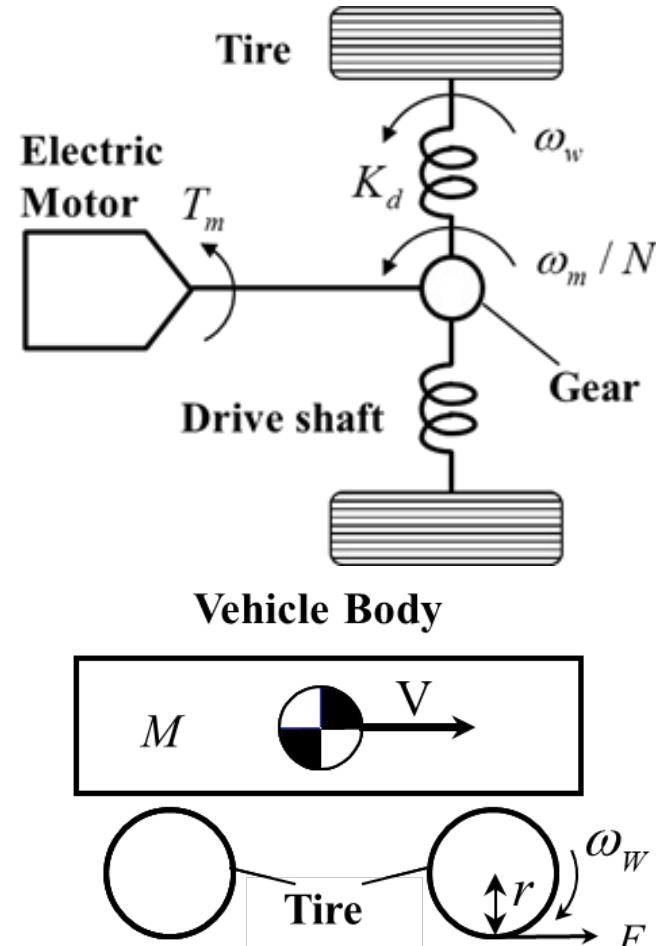
$m_2$ : sprung mass  
 $m_1$ : unsprung mass  
 $k_1$ : spring constant  
 $c_1$ : spring damping coefficient

$F_z$ : wheel load

$$F_z = (m_1 + m_2)g + c_1 \frac{d}{dt} (z_{m2} - z_t) + k_1 (z_{m2} - z_t)$$

## 2. Vertical vibration-Vertical vibration simulation model

- The longitudinal vehicle model mechanism is applied to electric-motor-driven vehicles.



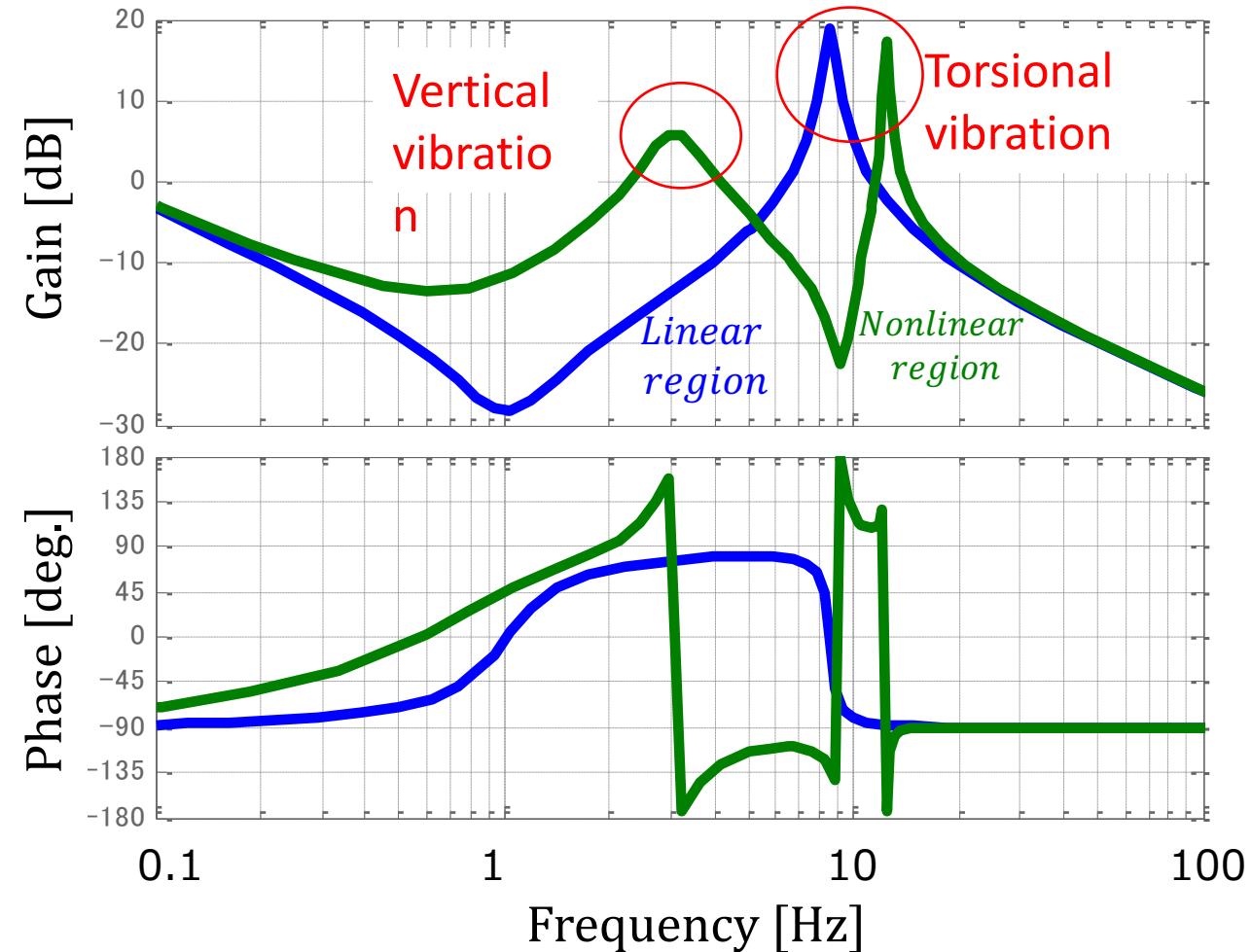
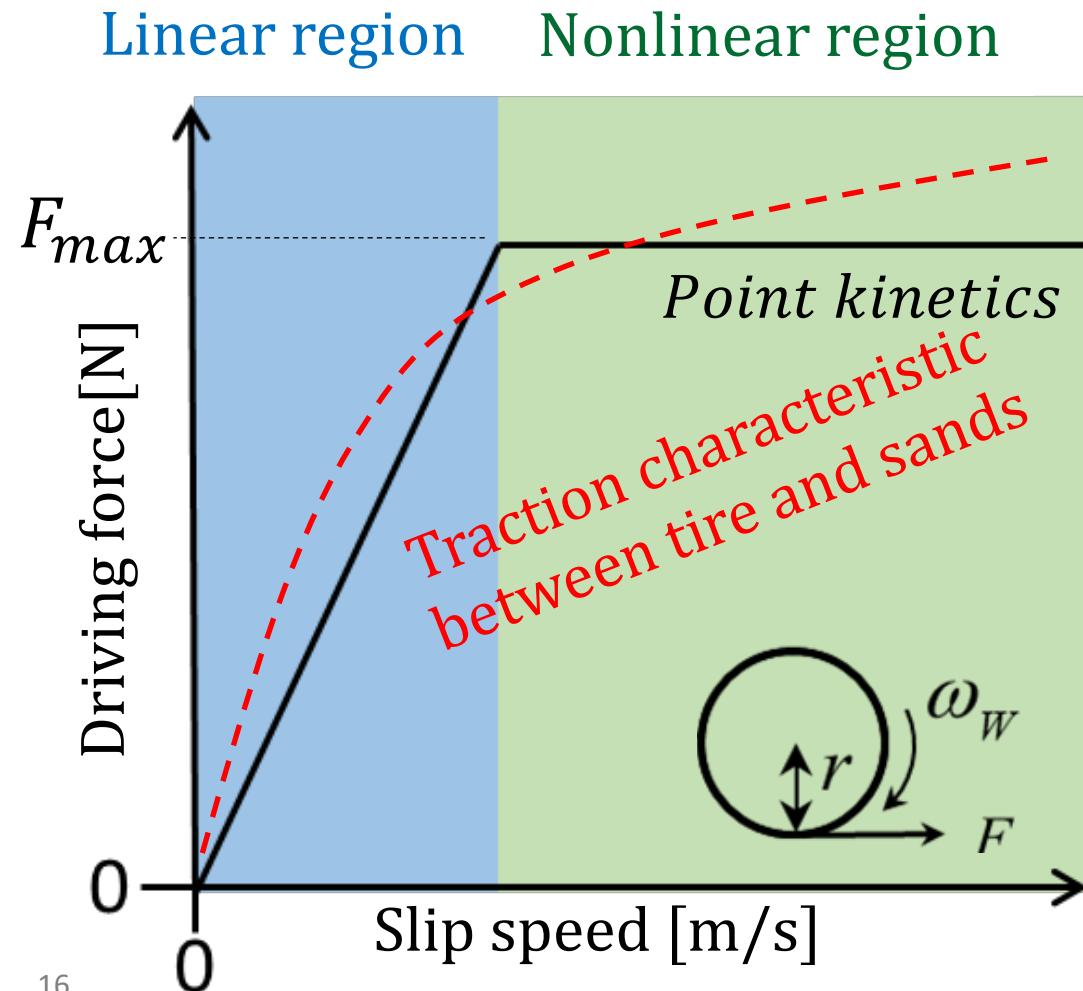
Equations	
Motor speed motion :	$J_m \frac{d}{dt} \omega_m = T_m - \frac{T_d}{N}$
Driveshaft speed motion :	$2J_W \frac{d}{dt} \omega_W = T_d - rF$
Forward and back movements:	$T_d = K_d \int \left( \frac{\omega_m}{N} - \omega_W \right) dt$
	$F = K_t(r\omega_W - V)$
	$M \frac{d}{dt} V = F - F_d$

Transmission characteristics of the motor speed based on torque:

$$G_p(s) = \frac{1}{s} \frac{\beta_3 s^3 + \beta_2 s^2 + \beta_1 s + \beta_0}{\alpha_3 s^3 + \alpha_2 s^2 + \alpha_1 s + \alpha_0}$$

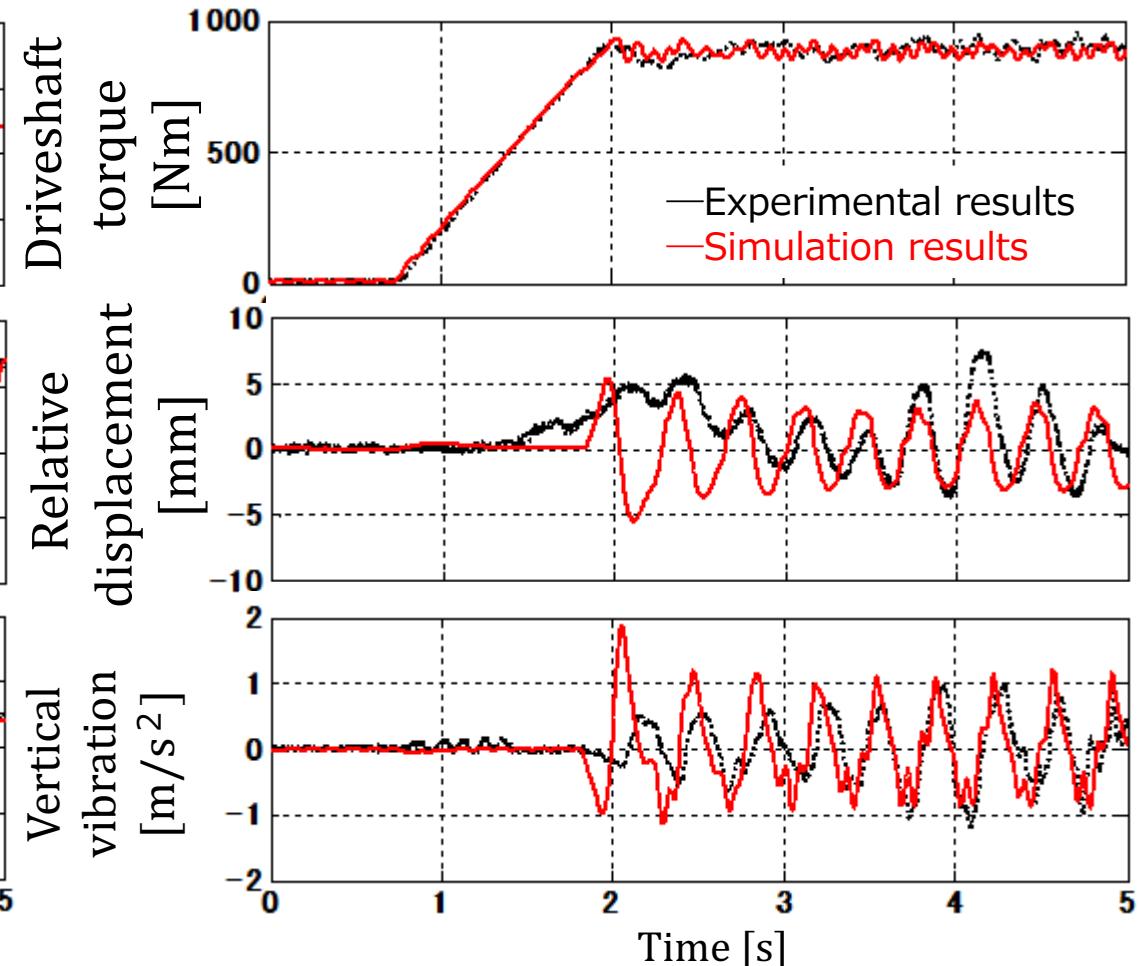
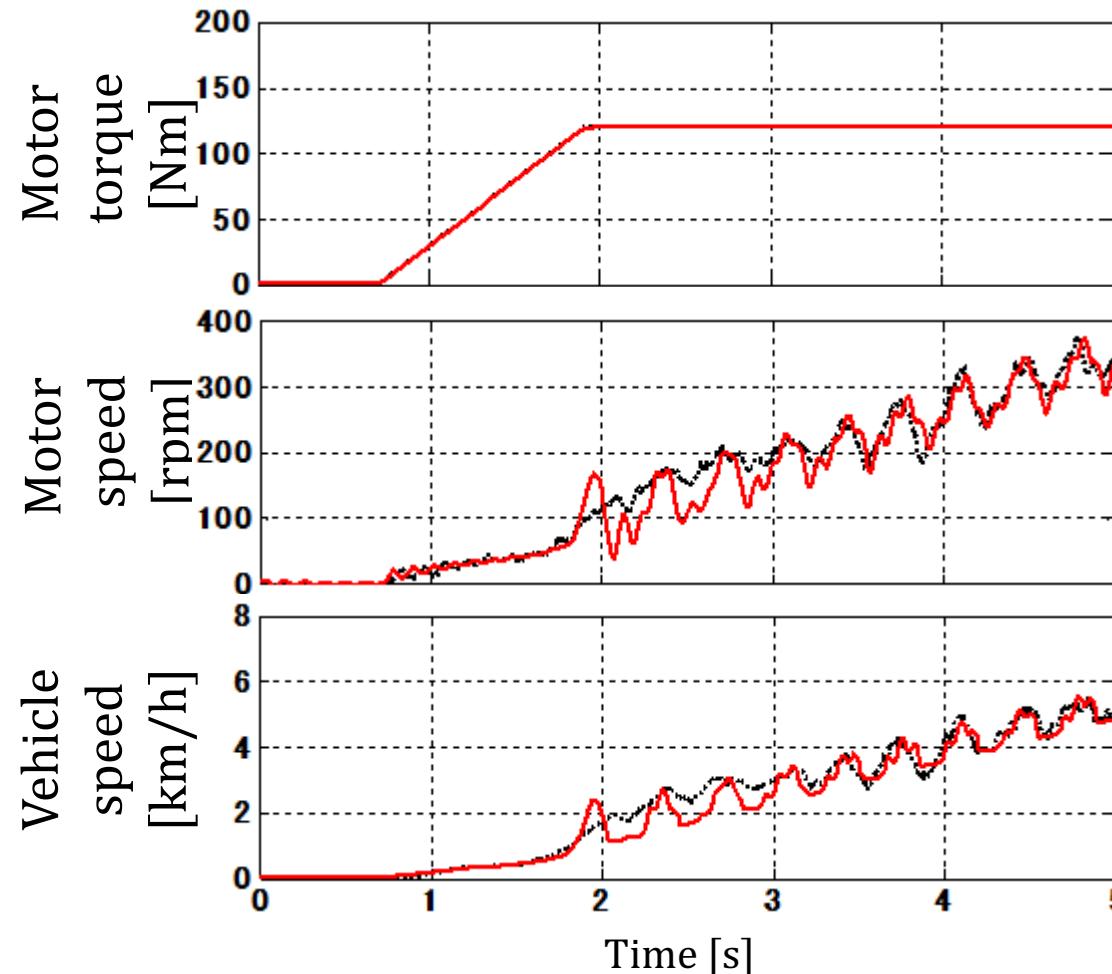
## 2. Vertical vibration-Vertical vibration simulation model

- In the linear region, the driving force increases according to slip.
- In the nonlinear region, the driving force is limited to the wheel load.



## 2. Vertical vibration-Vertical vibration simulation model

- Simulation results under the same experiment condition.
- Calibrating the motor speed fluctuations and vertical vibration.

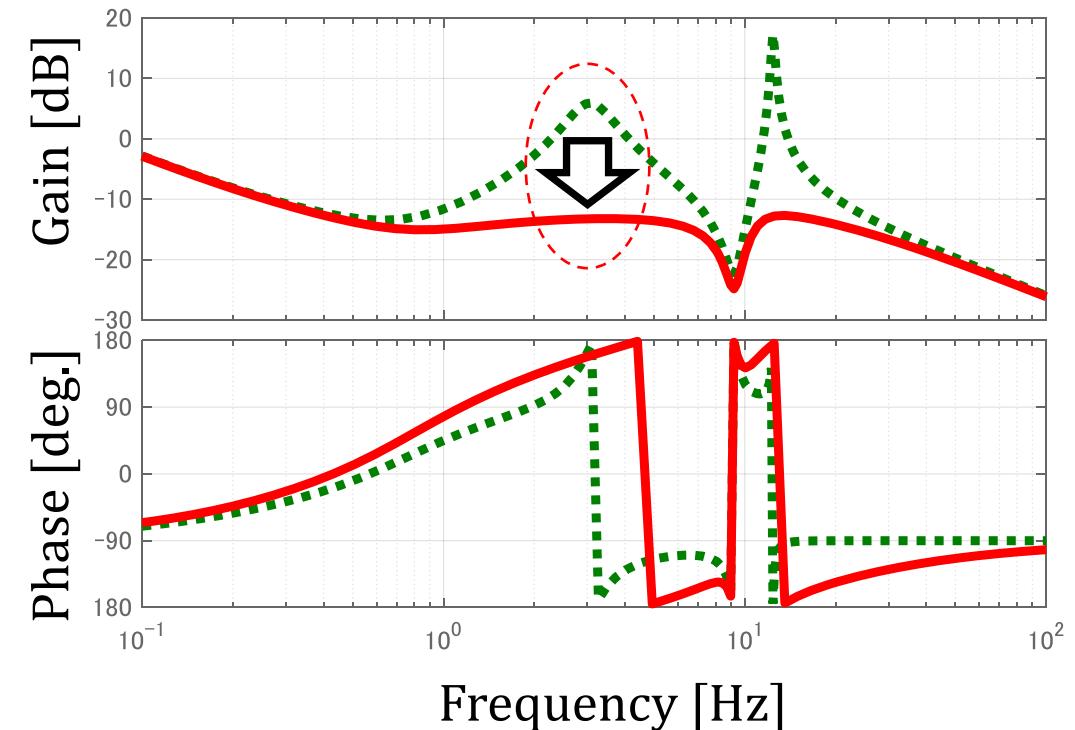
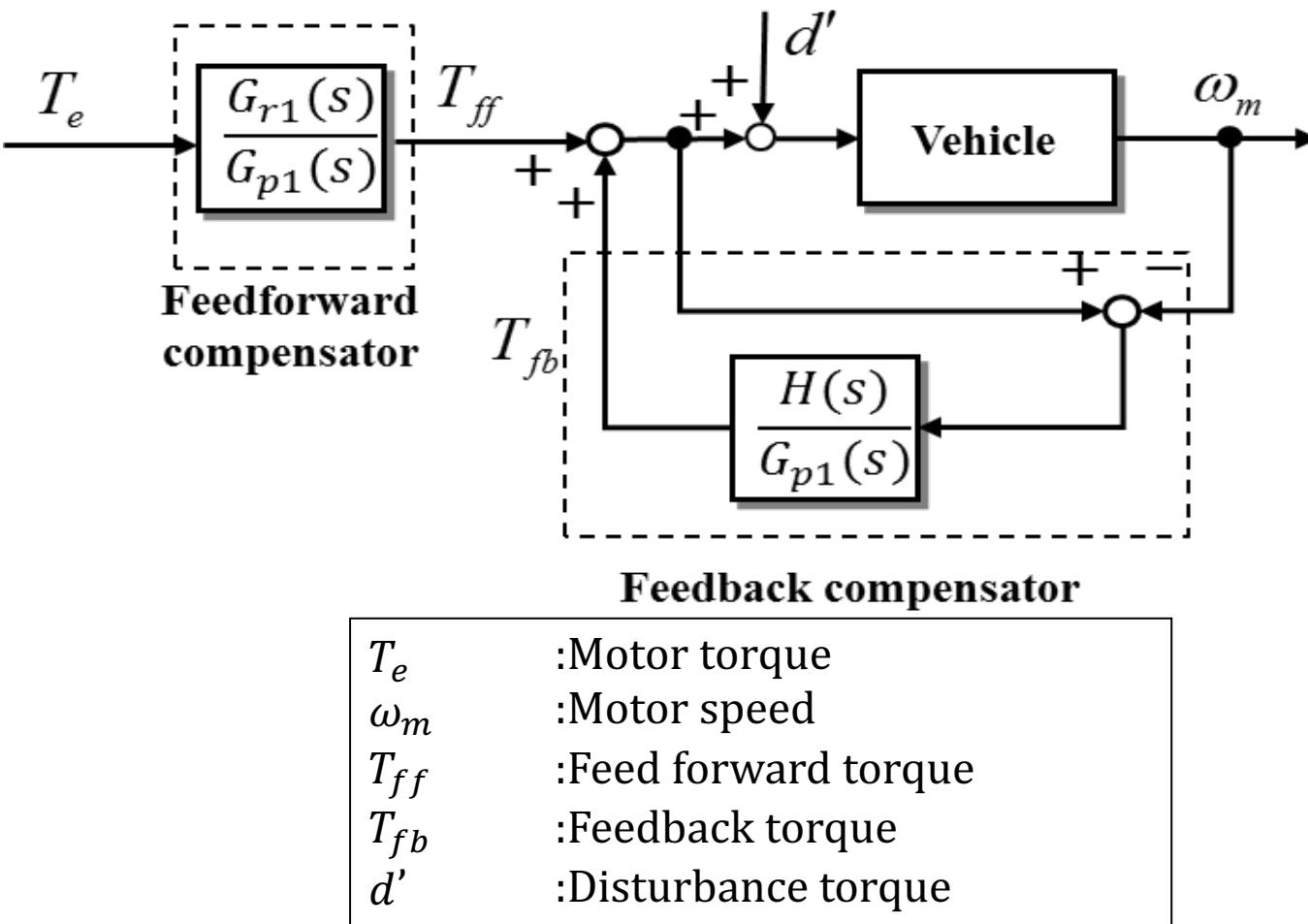


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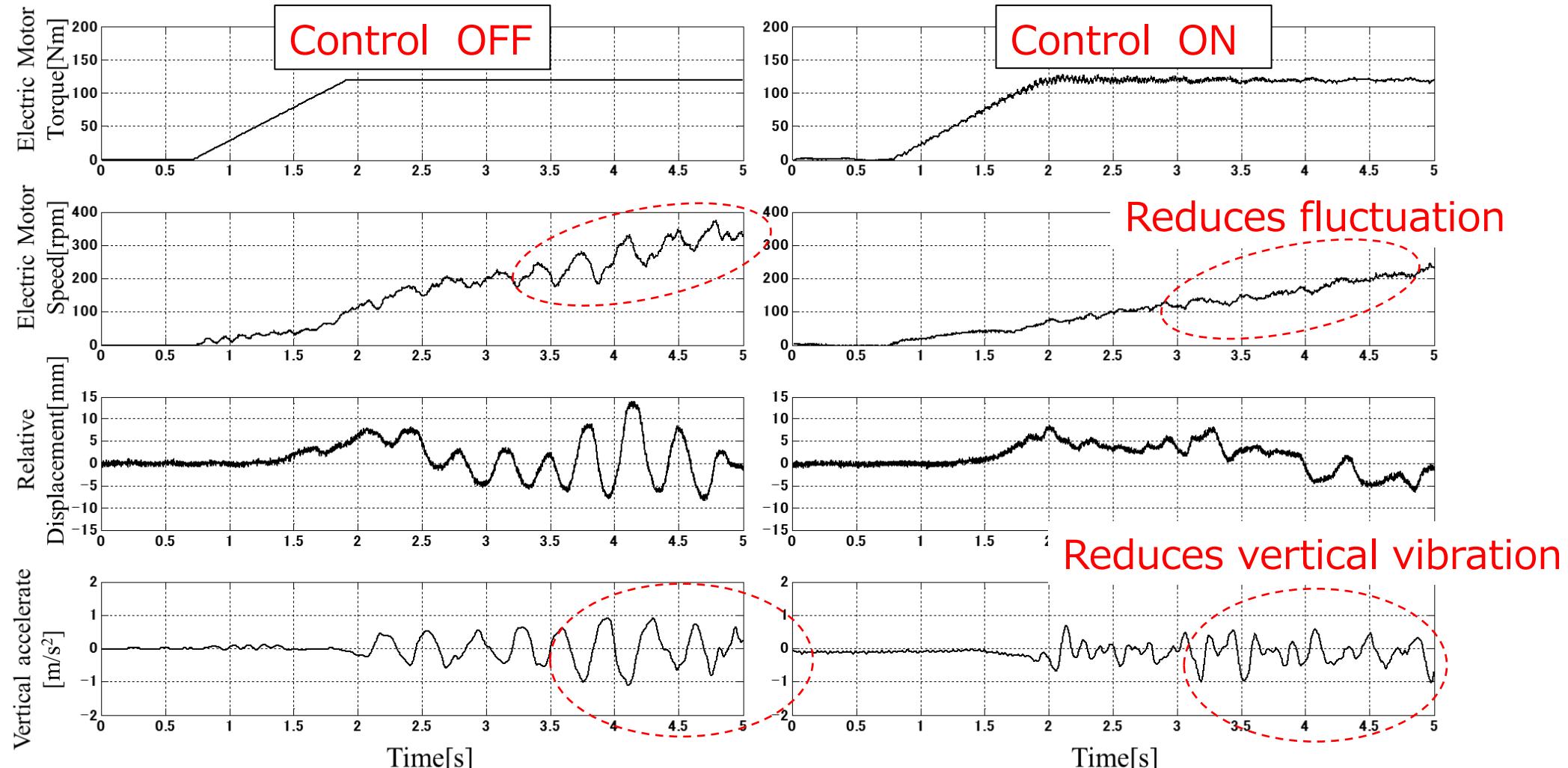
### 3. Vertical vibration motor control and effect

- Proposed vibration control for the dry sand condition
- Reducing the motor speed gain of vertical vibration frequency



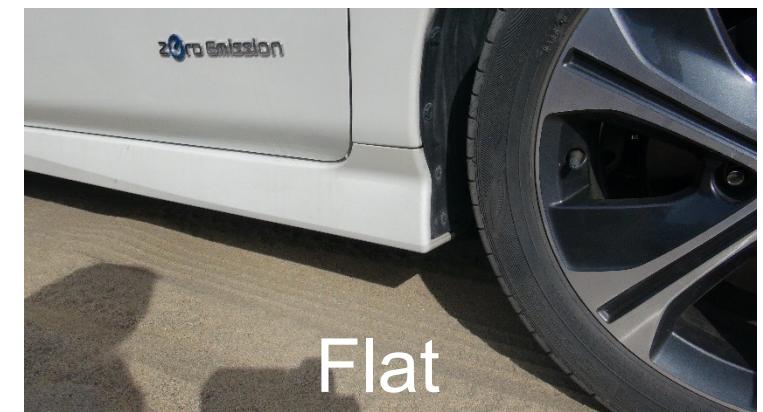
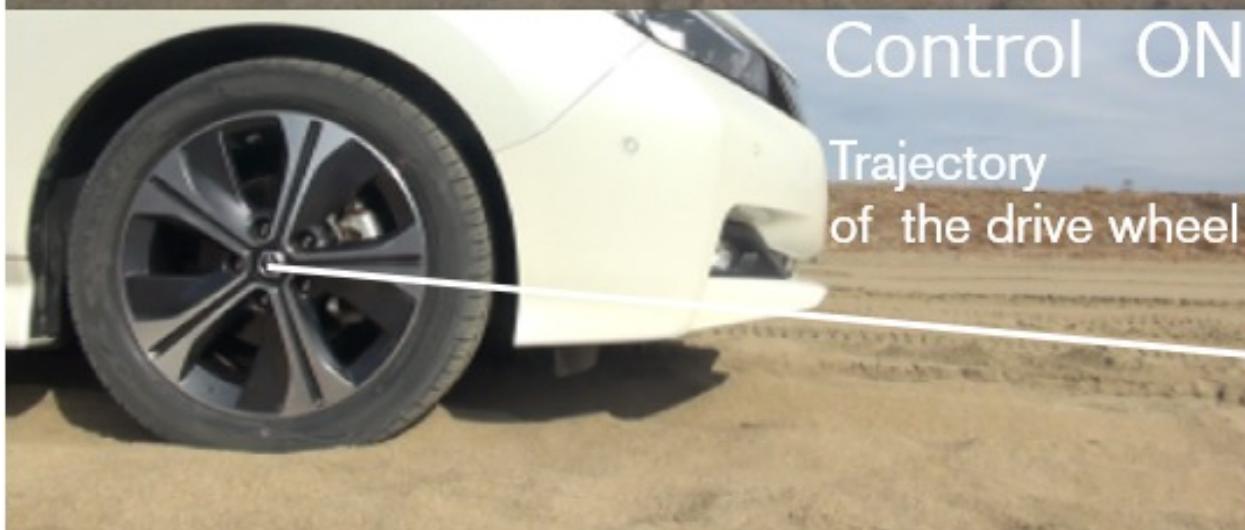
### 3. Vertical vibration motor control and effect

- Proposed vibration control effects on motor speed fluctuation reduction.
- In the result, low-frequency vertical vibration is reduced.



### 3. Vertical vibration motor control and effect

- To reduce vertical vibration using motor control



### 3. Vertical vibration motor control and effect

- Getting the same effect on deep snow as well.



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## 4. Summary

- The simulation model was designed based on the transient characteristics under dry sand condition.
- New electric motor control was proposed; it took motor speed fluctuations and vertical vibrations into account.
- Vertical vibration was reduced using the new control method under dry sand condition.

It realized the smooth running also under snow condition.

**Thank you for your attention**